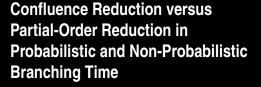
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Mark Timmer October 11, 2011



Joint work with Henri Hansen

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Formal Methods & Tools.



Why Confluence Reduction is Better than Partial-Order Reduction



in Probabilistic and Non-Probabilistic Branching Time

Mark Timmer October 11, 2011



Joint work with Henri Hansen

POR and confluence Implications Conclusions Questions

The context – probabilistic model checking

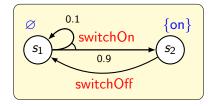
Probabilistic model checking:

- Verifying quantitative properties,
- Using a probabilistic model (e.g., an MDP)

The context – probabilistic model checking

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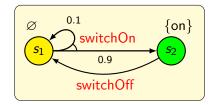
- Non-deterministically choose a transition
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Introduction

The context – probabilistic model checking

Probabilistic model checking:

- Verifying quantitative properties,
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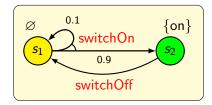
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POR and confluence Implications Conclusions Questions

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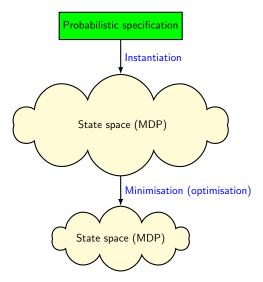
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- Probabilistically choose the next state

Main limitation (as for non-probabilistic model checking):

Susceptible to the state space explosion problem

Introduction Overview POR and confluence Comparison Implications Conclusions Questions

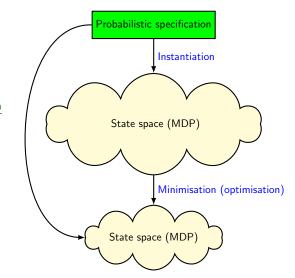
Combating the state space explosion



Introduction POR and confluence Implications Conclusions Questions

Combating the state space explosion

Optimised instantiation



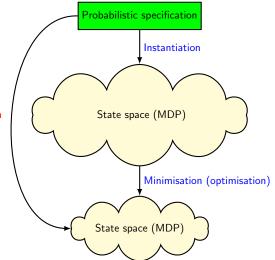
Introduction Overview POR and confluence

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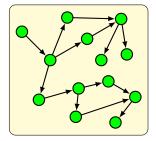
Optimised instantiation

- Partial-order reduction
- Confluence reduction (initially for PAs)



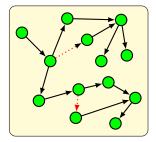
uction Overview POR and confluence Comparison Implications Conclusions Questions

Reductions – an overview



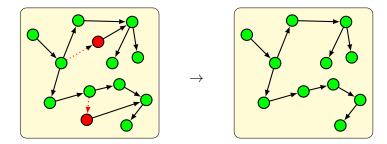
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Reductions – an overview

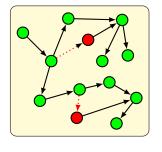


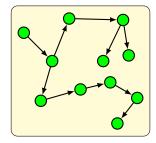
Overview POR and confluence Comparison Implications Conclusions Questions

Reductions – an overview





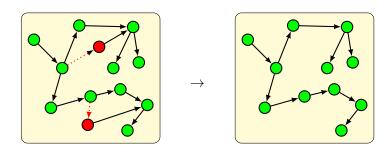




Reduction function:

$$R \colon S \to 2^{\Sigma}$$

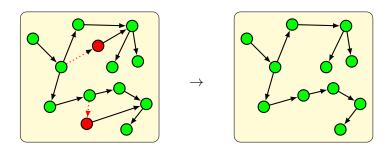
Reductions – an overview



Reduction function:

$$R: S \to 2^{\Sigma} \quad (R(s) \subseteq enabled(s))$$

Reductions – an overview



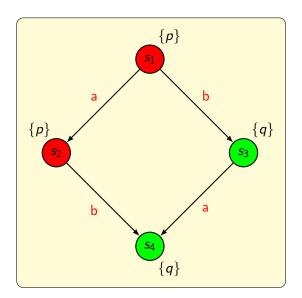
Reduction function:

$$R: S \to 2^{\Sigma}$$
 $(R(s) \subseteq enabled(s))$

If $R(s) \neq \text{enabled}(s)$, then R(s) consists of reduction transitions.

Overview POR and confluence Comparison Implications Conclusions Questions

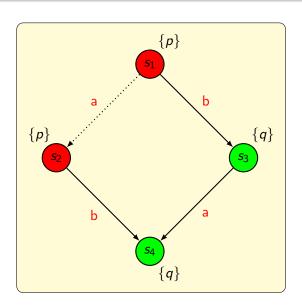
Basic concepts





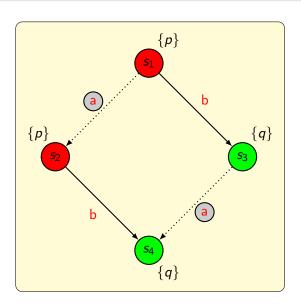
Overview POR and confluence Comparison Implications Conclusions Questions

Basic concepts



Stuttering transition:

No observable change

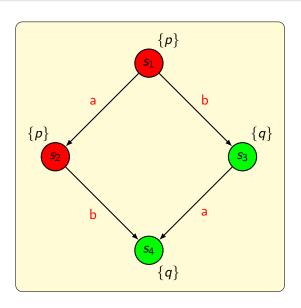


Stuttering transition:

No observable change

Stuttering action:

Yields only stuttering transitions

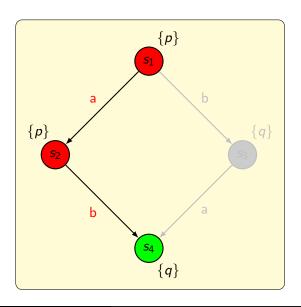


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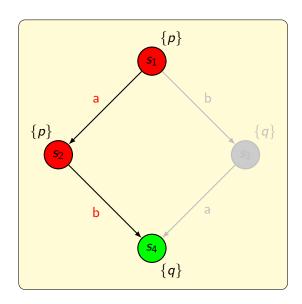


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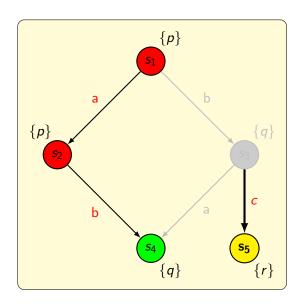
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$${p}{p}{q} =_{st} {p}{q}{q}$$



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 Yields only stuttering transitions

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Conclusions

- $LTL_{\setminus X}$ (linear time) Preservation of
- $CTL_{\setminus X}^*$ (branching time) Preservation of

Correctness criteria

- Preservation of (quantitative) LTL $_X$ (linear time)
- Preservation of (P)CTL* (branching time)

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- Preservation of (quantitative) $LTL_{\setminus X}$ (linear time)
- Preservation of (P)CTL^{*}_{\X} (branching time)

	Partial-order reduction	Confluence reduction
Linear time	[BGC'04, AN'04]	_
Branching time	[BAG'06]	[TSP'11]

Correctness criteria

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	Partial-order reduction	ı Co	onfluence reduction
Linear time	[BGC'04, AN'04]		_
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Overview POR and confluence Comparison Implications Conclusions Questions

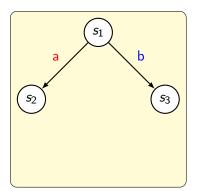
Partial-order reduction: ample sets

Partial-order reduction [Baier, D'Argenio, Größer, 2006]

• Based on independent actions and ample sets

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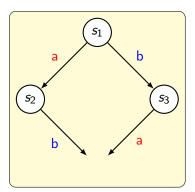
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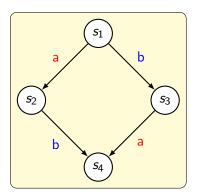
Independence of a and b:



Questions

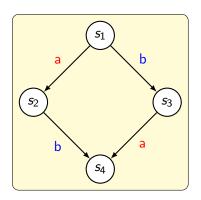
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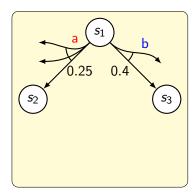
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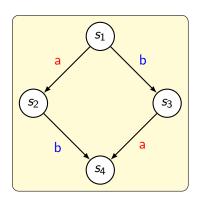
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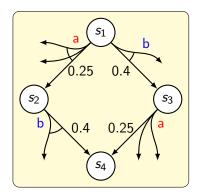




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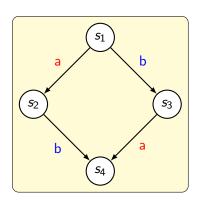


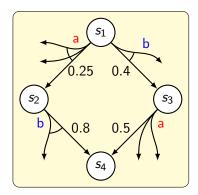
Implications

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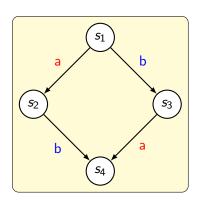
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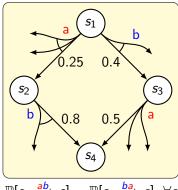




Partial-order reduction [Baier, D'Argenio, Größer, 2006]

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 $\mathbb{P}[s_1 \xrightarrow{ab} s] = \mathbb{P}[s_1 \xrightarrow{ba} s], \forall s$

Partial-order reduction [Baier, D'Argenio, Größer, 2006]

Based on independent actions and ample sets

Ample set conditions:

Given a reduction function $R: S \to 2^{\Sigma}$, for every $s \in S$



Questions

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A0 $\emptyset \neq R(s)$

A1

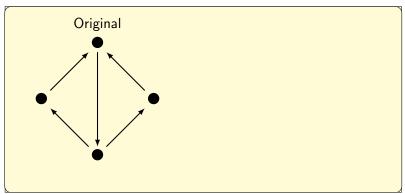
A2

A3

A4

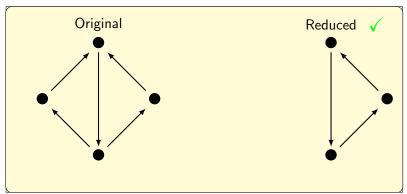
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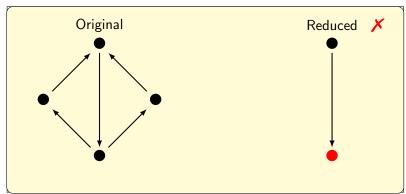
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Questions

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$$\varnothing \neq R(s)$$

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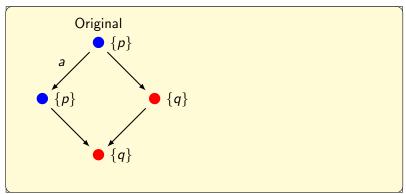
A2

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Based on independent actions and ample sets

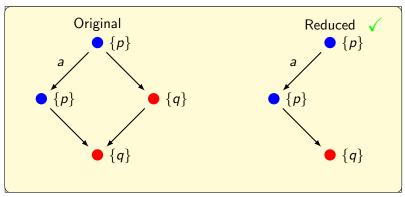


Questions

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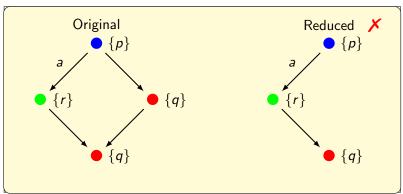
Based on independent actions and ample sets



Partial-order reduction [Baier, D'Argenio, Größer, 2006]

Based on independent actions and ample sets

Ample set conditions:



Questions

Questions

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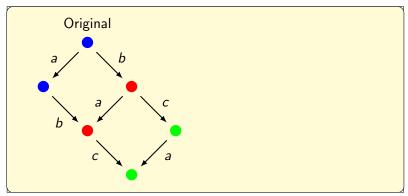
- A0 $\varnothing \neq R(s)$
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- A2 For every original path $s \xrightarrow{a_1} s_1 \xrightarrow{a_2} \dots \xrightarrow{a_n} s_n \xrightarrow{b} t$ such that $b \notin R(s)$ and b depends on R(s), there exists an i such that $a_i \in R(s)$

A3

A4

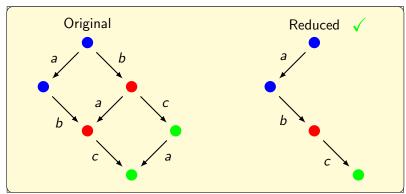
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Based on independent actions and ample sets



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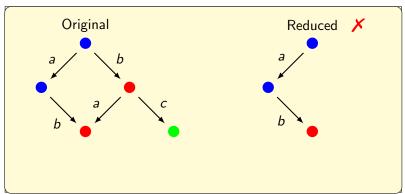
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Ample set conditions:



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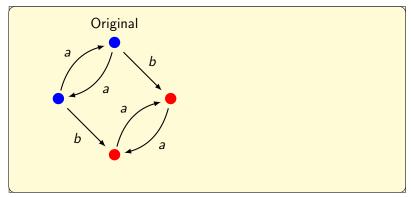
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A4

Partial-order reduction [Baier, D'Argenio, Größer, 2006]

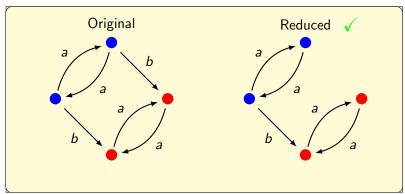
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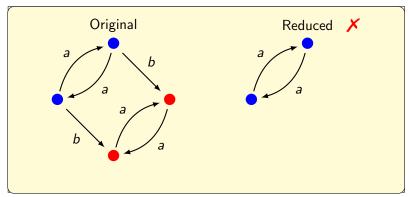


Conclusions

Questions

Partial-order reduction [Baier, D'Argenio, Größer, 2006]

Based on independent actions and ample sets



Questions

Partial-order reduction: ample sets

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Conclusions

Partial-order reduction: ample sets

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Overview POR and confluence Comparison Implications Conclusions Questions

Confluence

Confluence reduction [Timmer, Stoelinga, van de Pol, 2011]

• Based on equivalent distributions and confluent transitions

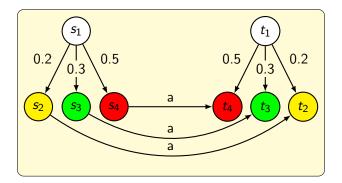
view POR and confluence Comparison Implications Conclusions Questions

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Based on equivalent distributions and confluent transitions

T-equivalent distributions



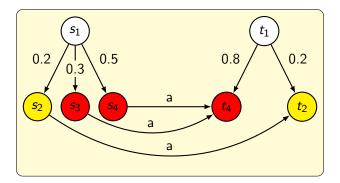
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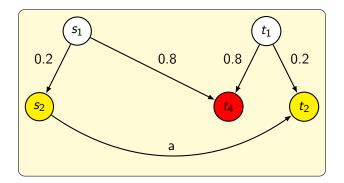
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Overview POR and confluence Comparison Implications Conclusions Questions

Confluence

Introduction

Confluence reduction [Timmer, Stoelinga, van de Pol, 2011]

Based on equivalent distributions and confluent transitions

The main idea:

- Choose a set T of transitions
- Make sure all of them are confluent
- R(s) = enabled(s) or $R(s) = \{a\}$ such that $(s \stackrel{a}{\rightarrow} t) \in T$

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- Make sure T is acyclic to prevent infinite postponing

Confluence

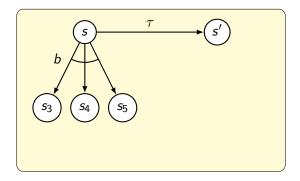
A set of transitions T is confluent if

- Every transition is labelled by a deterministic stuttering action
- If $s \xrightarrow{\tau} s' \in T$ and $s \xrightarrow{b} \mu$, then
 - **1** either $s' \xrightarrow{b} \nu$ and μ is T-equivalent to ν
 - 2 or $\mu(s') = 1$ (b deterministically goes to s')

Confluence

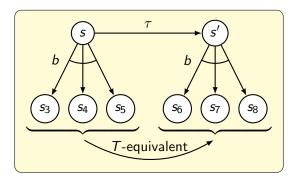
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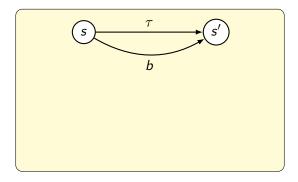


11 / 20

Confluence

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Overview POR and confluence Comparison Implications Conclusions Questions

Comparison



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Comparison

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Reduction transitions	Deterministic and stuttering

Comparison

Similarities among ample sets and confluence:

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Differences between ample sets and confluence:

POR For every original path $s \xrightarrow{a_1} s_1 \xrightarrow{a_2} \dots \xrightarrow{a_n} s_n \xrightarrow{b} t$ such that $b \notin R(s)$ and b depends on R(s), there exists an i such that $a_i \in R(s)$

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Conf If $s \xrightarrow{\tau} t$ and $s \xrightarrow{b} \mu$, then $\mu = \operatorname{dirac}(t)$ or $t \xrightarrow{b} \nu$ and μ is equivalent to ν .

Overview POR and confluence Comparison Implications Conclusions Questions

Comparison – POR implies Confluence

Theorem

Let R be a reduction function satisfying the ample set conditions. Then, all reduction transitions are confluent. Overview POR and confluence Comparison Implications Conclusions Questions

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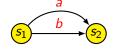
Proof (sketch).

- Take the set of all reduction transitions of the partial-order reduction.
- Recursively add transitions needed to complete the confluence diamonds
- Prove that the resulting set is indeed confluent.



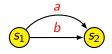
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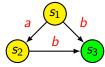
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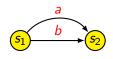
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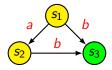


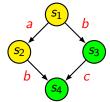


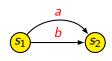
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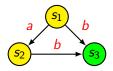
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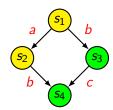


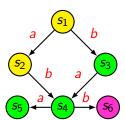






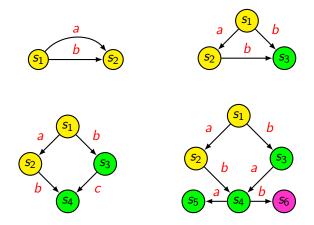






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Comparison – Confluence does not imply POR



POR's notion of independence is stronger than necessary.

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Strengthening of confluence

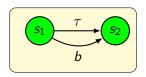
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Do not allow shortcuts

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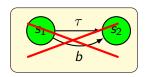
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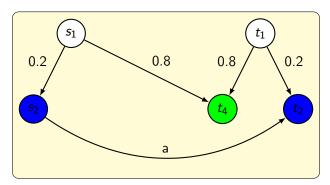


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Strengthening of confluence

- Do not allow shortcuts
- Do not allow overlapping distributions to be equivalent

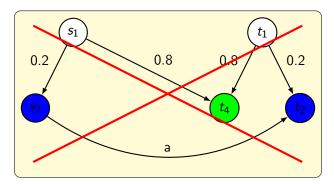
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Implications

Strengthening of confluence

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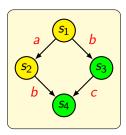
Strengthening of confluence

- Do not allow shortcuts
- Do not allow overlapping distributions to be equivalent
- Require action-separability

Implications

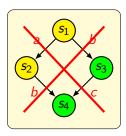
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POR and confluence Comparison Implications Conclusions Questions

Relaxing of partial-order reduction

We can change partial-order reduction in the following way:

• Relax the dependency condition

Implications

Relaxing of partial-order reduction

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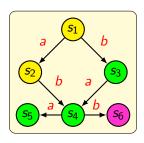
Relax the dependency condition

For every original path $s \xrightarrow{a_1} s_1 \xrightarrow{a_2} \dots \xrightarrow{a_n} s_n \xrightarrow{b} t$ such that $b \neq R(s)$ and R(s) depends on b at s, there exists an i such that $a_i \in R(s)$

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Strengthening of confluence

Theorem

Every acyclic strengthened confluence reduction is a relaxed ample set reduction.

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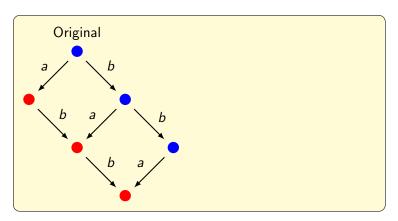
Corollary

In the non-probabilistic setting, the same statements hold: confluence is stronger than partial-order reduction, and the notions are equivalent for the adjusted definitions. n Overview POR and confluence Comparison Implications Conclusions Questions

Implications

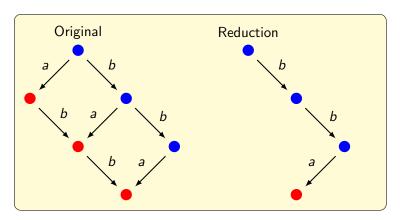


Implications

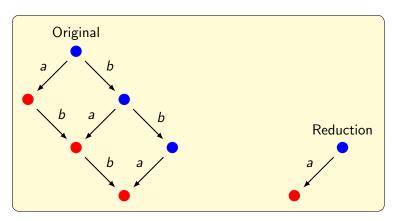


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Implications

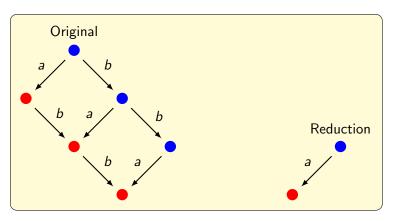


Implications



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Implications



- Representative in bottom strongly connected component
- Additional reduction of states and transitions
- No need for the cycle condition anymore!

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Conclusions

What to take home from this...

- We adapted the existing notion of confluence reduction to work in a state-based setting with MDPs.
- We proved that every ample set can be mimicked by a confluent set, but the the converse doesn't always hold.
- We showed how to make ample set reduction and confluence reduction equivalent
- We demonstrated one implication of our results, applying a technique from confluence reduction to POR
- The results are independent of specific heuristics, and also hold non-probabilistically

POR and confluence Comparison Implications Conclusions

Conclusions

What to take home from this...

- We adapted the existing notion of confluence reduction to

- And: finally people have a reason to like confluence better! hold non-probabilistically

Questions

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Questions

Questions?

A paper, containing all details and proofs, can be found at http://wwwhome.cs.utwente.nl/~timmer/research.php